

Assignment 2 - Pumping Lemma

Due Tue Feb 3, 2026

1. Prove that the following language is not regular.

$$L_1 = \{ w \in \{ \#, 0, 1 \}^* \mid w = x \# y \text{ where } x \text{ and } y \text{ are binary encodings of integers } n_x \text{ and } n_y, \text{ respectively, with at least one leading } 0, \text{ and } n_x < n_y. \}$$

Example: $011 \# 001101 \in L_1$.

$n_x = 3$ $n_y = 9$

Hint: Closure theorems can be used effectively here.

2. Prove that the class RL of regular languages is closed under Reverse ... i.e show that

8 if L is regular, so is L^R where

$$L^R = \{ w^R \mid w \in L \}$$

3. Prove using the Pumping Lemma that $L_3 = \{ a^i b^j c^k \mid i \geq j+k \}$ is not regular.

4. give a CFG for the language

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$$L_3 = \{a^i b^j c^k \mid i \geq j+k\}$$