## Association Rules. Apriori algorithm

Data mining lab 7. Part I

## Association rules generation

- Step 1. Find all frequent itemsets $\mathrm{Fi}, 2<=\mathrm{i}<=\mathrm{T}$, T -total number of items
- Step 2. Generate rules from the frequent itemsets


## Tutorial exercise 1. Frequent itemsets

Find all frequent itemsets from the following data. Minsupport $=2$.

Pizza toppings dataset:

| Order ID | Extra cheese | Onions | Peppers | Mushrooms | Olives | Anchovy |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 1 |  |  | 1 |  |
| 2 |  |  | 1 | 1 |  |  |
| 3 |  | 1 |  |  |  | 1 |
| 4 | 1 |  |  | 1 |  |  |
| 5 | 1 | 1 |  | 1 | 1 |  |
| 6 | 1 | 1 |  | 1 |  |  |

Binary data format

## 1. Replace item names by codes

| Order ID | A | B | C | D | E | F |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 |  |  | 1 |  |
| 2 |  |  | 1 | 1 |  |  |
| 3 |  | 1 |  |  |  | 1 |
| 4 | 1 |  | 1 |  |  |  |
| 5 | 1 | 1 | 1 | 1 |  |  |
| 6 | 1 | 1 | 1 |  |  |  |

## 2. Count 1-item frequent itemsets F1

|  | A | B | C | D | E | F |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 1 | 1 |  |  | 1 |  |
|  |  |  | 1 | 1 |  |  |
|  | 1 |  |  | 1 |  |  |
|  | 1 | 1 |  | 1 | 1 |  |
|  | 1 | 1 |  | 1 |  |  |
| Total (s): | 4 | 4 |  | 4 | 2 | 1 |

## 3. Generate candidate 2-item frequent itemsets C2

|  | A | B | D | E |
| :--- | :--- | :--- | :--- | :--- |
| A |  |  |  |  |
| B |  |  |  |  |
| D |  |  |  |  |
| E |  |  |  |  |

$C 2:\{\{A, B\},\{A, D\},\{A, E\},\{B D\},\{B, E\},\{D, E\}\}$

## 4. Verify counts of C 2 by counting

| Order ID | A | B | C | D | E | F |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 |  |  | 1 |  |
| 2 |  |  | 1 | 1 |  |  |
| 3 |  | 1 |  |  |  | 1 |
| 4 | 1 |  | 1 |  |  |  |
| 5 | 1 | 1 | 1 | 1 |  |  |
| 6 | 1 | 1 | 1 |  |  |  |


|  | A | B | D | E |
| :--- | :--- | :--- | :--- | :--- |
| A |  | 3 | 3 | 2 |
| B |  |  | 2 | 2 |
| D |  |  |  | 1 |
| E |  |  |  |  |

F2=\{\{A,B\},\{A,D\},\{A,E\},\{B,D\},\{B,E\})

# 5. Generate candidate 3-item frequent itemsets C3 

$F 2=\{\{A, B\},\{A, D\},\{A, E\},\{B, D\},\{B, E\})$

|  | A,B | A,D | A,E | B,D | B,E |
| :--- | :--- | :--- | :--- | :--- | :--- |
| A,B |  |  |  |  |  |
| A,D |  |  |  |  |  |
| A,E |  |  |  |  |  |
| B,D |  |  |  |  |  |
| B,E |  |  |  |  |  |

3-items frequent itemsets must share 3-2=1 item

$$
C 3=\{\{A, B, D\},\{A, B, E\},\{A, D, E\},\{B, D, E\}\}
$$

# 6. Prune C 2 based on F2 

$F 2=\{\{A, B\},\{A, D\},\{A, E\},\{B, D\},\{B, E\})$<br>$C 3=\{\{A, B, D\},\{A, B, E\},\{A, D, E\},\{B, D, E\}\}$<br>Pruned, since subset $\{D, E\}$ is infrequent
$C 3$ after pruning $=\{\{A, B, D\},\{A, B, E\}\}$

## 7. Verify 3-item itemsets counts generate F3

| Order ID | A | B | C | D | E | F |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  | 1 | 1 |  |  |  | 1 |  |
| 2 |  |  |  | 1 |  | 1 |  |  |
| 3 |  |  | 1 |  |  |  |  |  |
| 4 | 1 |  |  |  |  | 1 |  |  |
| 5 |  | 1 | 1 |  |  | 1 |  | 1 |
|  |  | 1 |  | 1 |  |  | 1 |  |

$F 3=\{\{A, B, D\},\{A, B, E\}\}$

# 8. Generate 4-item candidate frequent itemsets C4 

The only possible 4-items itemset from $F 3=\{\{A, B, D\},\{A, B, E\}\}$ is $C 4=\{A, B, D, E\}$

Prune C4 using F3
$F 3=\{\{A, B, D\},\{A, B, E\}\}$
$\{A, B, D, E\}$ is pruned since its subset $\{B, D, E\}$ is infrequent

## 9. Report frequent 2-3 itemsets:

$$
\begin{aligned}
& \mathrm{F} 2=\{\{\mathrm{A}, \mathrm{~B}\},\{\mathrm{A}, \mathrm{D}\},\{\mathrm{A}, \mathrm{E}\},\{\mathrm{B}, \mathrm{D}\},\{\mathrm{B}, \mathrm{E}\}) \\
& \mathrm{F} 3=\{\{\mathrm{A}, \mathrm{~B}, \mathrm{D}\},\{\mathrm{A}, \mathrm{~B}, \mathrm{E}\}\}
\end{aligned}
$$

| Order ID | Extra <br> cheese | Onions | Peppers | Mushrooms | Olives | Anchovy |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 |  |  | 1 |  |
| 2 |  |  | 1 | 1 |  |  |
| 3 |  | 1 |  |  |  | 1 |
| 4 | 1 |  | 1 |  |  |  |
| 5 | 1 | 1 | 1 | 1 |  |  |
| 6 | 1 | 1 | 1 |  |  |  |

Customers buy following toppings together:
\{extra cheese, onions, mushrooms\}, \{extra cheese, onions, olives\} etc

## 10. Designing code for Apriori

## General pseudocode

```
F1 = {frequent 1-item sets};
k = 2;
while( F F-1 is not empty )
{
    Ck}=\mathrm{ Apriori_generate( Fk-1 );
    Ck}=\mathrm{ Apriori_prune( Ck );
    for all transactions t in T
        {Subset( Ck, t );}
    Fk= { c in Ck s.t. c.count >=minimum_support};
    k++;
}
```

Answer = union of all sets $\mathrm{F}_{\mathrm{k}}$;

# 11. Generating 1-frequent itemset (in map_reduce framework). Map 

## Local test

```
def fun_map_1(e,params):
    delimiter=params['delimiter']
    count_map={}
    for row in e.split('\n'):
        transactions=row.split(delimiter)
        Map returns pairs (item id,1)
        for i in range (0,len(transactions)):
        if transactions[str(i)]==1:
        count_map[str(i)]=1
```

return [ (i,count) for i,count in count_map.iteritems()]

## 12. Generating 1-frequent itemset (in a map_reduce framework). Reduce

Local test

```
def fun_reduce1(iter, out, params):
    count_dict = {}
    min_supp=params['min_support']
    for i, count in iter:
    if i not in count_dict:
        count_dict[i]=int(count)
    else:
        count_dict[i]+=int(count)
```

    for i, total in count_dict.iteritems():
    if total>=min_supp
        out.add(i, total)
    Reduce adds counts for each item and adds them to the output list if the count is at least min_supp

## Disco session

mgbarsky@mgbarsky-pc:~\$ ssh -L 7000:db101a:7000 dbssh1.cs.uvic.ca
mgbarsky@dbssh1.cs.uvic.ca's password:
[mgbarsky@db101a ~]\$ wget http://webhome.cs.uvic.ca/~mgbarsky/inputs/marketbasket.csv [mgbarsky@db101a ~]\$ wget http://webhome.cs.uvic.ca/~mgbarsky/dmlabs/ficount.py [mgbarsky@db101a ~]\$ sudo distrfiles marketbasket.csv 200 Password:
[mgbarsky@db101a ~]\$ sudo discorun ficount.py `cat marketbasket.csv.chunks` > result_data
[ OK ]

## Monitoring the cluster

## http://localhost:7000



[^0]
## Monitoring your job

job:
frequent_itemsets@1236565216
[delete job records] [delete all job data]

| Job info |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Job is ready <br> started: 2009/03/08 19:20:17 |  |  |  |  |
|  | Waiting | Running | Done | Failed |
| Map | 0 | 0 | 10 | 0 |
| Reduce | 0 | 0 | 5 | 0 |


| Current nodes |
| :--- |
|  |
|  |
|  |
|  |


| Map Inputs |
| :--- |
| disco://db204a/mgbarsky.part_market |
| disco://db108a/mgbarsky.part_market |
| disco://db109a/mgbarsky.part_market |
| disco://db205a/mgbarsky.part_market |
| disco://db201a/mabarsky.part market |
| 4 |

## Results <br> dir://db201a/reduce/frequent_itemset ${ }^{\bullet}$ <br> dir://db301a/reduce/frequent_itemset: dir://db107a/reduce/frequent_itemset: dir://db207a/reduce/frequent_itemset dir://db309a/reduce/frequent itemset/.

Filter: $\qquad$ show

2009/03/08 19:20:17 master READY
2009/03/08 19:20:17 master
Reduce phase done


2009/03/08 19:20:17 master
Received results from reduce:4 @ db201a.

## 2009/03/08 19:20:17 db201a

[reduce:4] Worker done
2009/03/08 19:20:17 db201a
[reduce:4] Reduce done

## Results

Starting Disco job
Job 1 done. Result
21636
21792
6630
21556
21263
21340
21085
21110
21415
21834

## 13. To do

- The output of fun_reduce1 is a list of tuples
- Lexicographically order list by item id
- Combine 1-itemsets into 2-itemsets - generate C2 in form of the dictionary $\mathrm{C} 2=\{($ item 1 , item2), 0$\}$
- No pruning since each set has only 2 subsets and both are frequent
- Implement fun_map2 which takes the same input and C2 as a parameter. It counts for each transaction the number of co-occurrence of item1 and item2.
- The output of fun_map2 is reduced into frequent 2item itemset F2


## Output- F2. Min_support=60

| $(' 110 ', ~ ' 238 ') 64$ | Tangerines, Creamy Peanut Butter |
| :--- | :--- |
| $(' 132 ', ~ ' 16 ') 66$ | Chicken Soup, Vanilla Ice Cream |
| $(' 132 ', ~ ' 141 ') 75$ | Chicken Soup, Blueberry Waffles |
| $(' 141 ', ~ ' 4 ') 67$ | Blueberry Waffles, Frozen Chicken Wings |
| $(' 141 ', ' 175 ') 65$ | Blueberry Waffles, Microwave Popcorn |
| $(' 124 ', ~ ' 141 ') 70$ | Bologna, Blueberry Waffles |
| $(' 124 ', ~ ' 132 ') 71$ | Bologna, Chicken Soup |
| $(' 132 ', ' 238 ') 61$ | Chicken Soup, Creamy Peanut Butter |
| $(' 124 ', ~ ' 16 ') 61$ | Bologna, Vanilla Ice Cream |
| $(' 141 ', ~ ' 16 ') 70$ | Blueberry Waffles, Vanilla Ice Cream |
| $(' 132 ', ~ ' 175 ') 61$ | Chicken Soup, Microwave Popcorn |
| $(' 201 ', ~ ' 4 ') 66$ | Frozen Peas, Frozen Chicken Wings |
| $(' 132 ', ~ ' 4 ') 62$ | Chicken Soup, Frozen Chicken Wings |

Setting min_support high we possible miss all the interesting associations


[^0]:    

