# Attribute types, concept hierarchies and negative associations 

Lecture 17

## Types of attributes

- We were working with asymmetric binary attributes:
- Binary: Item: 0 - not present, 1 - present
- Asymmetric: more interested in presence than in absence
- What do we do if attributes are
- Symmetric binary
- Categorical
- Numeric


## Attribute type examples

- Symmetric binary attributes
- Gender
- Computer at Home
- Chat Online
- Shop Online
- Privacy Concerns

Internet survey data with categorical attributes.

| Gender | Level of <br> Education | State | Computer <br> at Home | Chat <br> Online | Shop <br> Online | Privacy <br> Concerns |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Female | Graduate | Illinois | Yes | Yes | Yes | Yes |
| Male | College | California | No | No | No | No |
| Male | Graduate | Michigan | Yes | Yes | Yes | Yes |
| Female | College | Virginia | No | No | Yes | Yes |
| Female | Graduate | California | Yes | No | No | Yes |
| Male | College | Minnesota | Yes | Yes | Yes | Yes |
| Male | College | Alaska | Yes | Yes | Yes | No |
| Male | High School | Oregon | Yes | No | No | No |
| Female | Graduate | Texas | No | Yes | No | No |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |

## Attribute type examples

- Nominal (categorical) attributes
- Level of Education
- State

Internet survey data with categorical attributes.

| Gender | Level of <br> Education | State | Computer <br> at Home | Chat <br> Online | Shop <br> Online | Privacy <br> Concerns |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Female | Graduate | Illinois | Yes | Yes | Yes | Yes |
| Male | College | California | No | No | No | No |
| Male | Graduate | Michigan | Yes | Yes | Yes | Yes |
| Female | College | Virginia | No | No | Yes | Yes |
| Female | Graduate | California | Yes | No | No | Yes |
| Male | College | Minnesota | Yes | Yes | Yes | Yes |
| Male | College | Alaska | Yes | Yes | Yes | No |
| Male | High School | Oregon | Yes | No | No | No |
| Female | Graduate | Texas | No | Yes | No | No |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |

## Transforming attributes into asymmetric binary

- Create a new item for each distinct attribute-value pair.
- E.g., the nominal attribute Level of Education can be replaced by three binary items:
- Education = College
- Education = Graduate
- Education = High School
- Binary attributes such as Gender are converted into a pair of binary items
- Male
- Female


## Data after binarizing attributes into "items"

| Male | Female | Education <br> = Graduate | Education <br> = College | $\cdots$ | Privacy <br> = Yes | Privacy <br> = No |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1 | 1 | 0 | $\cdots$ | 1 | 0 |
| 1 | 0 | 0 | 1 | $\cdots$ | 0 | 1 |
| 1 | 0 | 1 | 0 | $\cdots$ | 1 | 0 |
| 0 | 1 | 0 | 1 | $\cdots$ | 1 | 0 |
| 0 | 1 | 1 | 0 | $\cdots$ | 1 | 0 |
| 1 | 0 | 0 | 1 | $\cdots$ | 1 | 0 |
| 1 | 0 | 0 | 1 | $\cdots$ | 0 | 1 |
| 1 | 0 | 0 | 0 | $\cdots$ | 0 | 1 |
| 0 | 1 | 1 | 0 | $\cdots$ | 0 | 1 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\cdots$ | $\cdots$ | $\ldots$ |

Note, that here we are interested in both yes and no values of binary attributes, so we generate a separate item for each: privacy=Yes and privacy=No

## Numeric (continuous) attributes

- Solution: Discretize
- Example of rules:
- Age $\in[21,35) \wedge$ Salary $\in[70 k, 120 k) \rightarrow$ Buy
- Salary $\in[70 k, 120 k) \wedge$ Buy $\rightarrow$ Age: $\mu=28, \sigma=4$
- Of course discretization isn't always easy.
- If intervals too large may not have enough confidence Age $\in[12,36$ ) $\rightarrow$ Chat Online $=$ Yes ( $s=30 \%, c=57.7 \%$ ) (minconf=60\%)
- If intervals too small may not have enough support Age $\in[16,20$ ) $\rightarrow$ Chat Online $=$ Yes ( $s=4.4 \%, c=84.6 \%$ ) (minsup=15\%)


## Statistics-based quantitative association rules

Salary $\in[70 k, 120 k) \wedge$ Buy $\rightarrow$ Age: $\mu=28, \sigma=4$
Generated as follows:

- Specify the target attribute (e.g. Age).
- Withhold target attribute, and "itemize" the remaining attributes.
- Extract frequent itemsets from the itemized data.
- Each frequent itemset identifies an interesting segment of the population.
- Derive a rule for each frequent itemset.
- E.g., the preceding rule is obtained by averaging the age of Internet users who support the frequent itemset
\{Annual Income> \$100K, Shop Online = Yes\}
- Remark: Notion of confidence is not applicable to such rules.


## Associations across concept hierarchies

## Items: levels of abstraction



## Multi-level Association Rules

- Rules about items at lower levels of abstraction can represent a more general rule:
skim milk $\rightarrow$ white bread,
$2 \%$ milk $\rightarrow$ wheat bread,
skim milk $\rightarrow$ wheat bread, etc.
are all indicative of association between their generalizations milk and bread


## How much to generalize?

- Should we consider correlation between milk and bread, between cream and bagels, or between specific labels of cream and bagels?
- The correlation between specific items can be hard to find because of the low support
- The correlation between more general itemsets can be very low, despite that the support is high


## Mining multi-level Association Rules

## Approach 1

- Augmenting each transaction with higher level items

Original Transaction: \{skim milk, wheat bread\}
Augmented Transaction:
\{skim milk, wheat bread, milk, bread, food\}

- Issue:
- Items that reside at higher levels have much higher support counts
if support threshold is low, we get too many frequent patterns involving items from the higher levels


## Multi-level Association Rules

## Approach 2

- Generate frequent patterns at highest level first.
- Then, generate frequent patterns at the next highest level, and so on, decreasing minsupport threshold
- Issues:
- May miss some potentially interesting cross-level association patterns.
E.g.
skim milk $\rightarrow$ white bread, 2\% milk $\rightarrow$ white bread, skim milk $\rightarrow$ white bread
might not survive because of low support, but milk $\rightarrow$ white bread could. However, we don't generate a cross-level itemset such as \{milk, white bread\}


## Transactions also may have hierarchies



Hierarchy of groups: strata

## Example (symmetric binary variables)

| Buy | Buy Exercise Machine |  |  |
| :---: | :---: | :---: | :---: |
|  | Yes | No |  |
| Yes | 99 | 81 | 180 |
| No | 54 | 66 | 120 |
|  | 153 | 147 | 300 |

- What's the confidence of the following rules: (rule 1) $\{$ HDTV $=$ Yes $\} \rightarrow$ \{Exercise machine $=$ Yes $\}$
(rule 2) $\{\mathrm{HDTV}=\mathrm{No}\} \rightarrow$ \{Exercise machine $=\mathrm{Yes}\}$ ?
Confidence of rule $1=99 / 180=55 \%$
Confidence of rule $2=54 / 120=45 \%$
Conclusion: there is a positive correlation between buying HDTV and buying exercise machines


## What if we look into more specific groups

| Customer | Buy | Buy Exercise Machine |  | Total |
| :--- | :---: | :---: | :---: | :---: |
| Group | HDTV | Yes | No |  |
| College Students | Yes | 1 | 9 | 10 |
|  | No | 4 | 30 | 34 |
| Working Adult | Yes | 98 | 72 | 170 |
|  | No | 50 | 36 | 86 |

- What's the confidence of the rules for each strata: (rule 1) $\{$ HDTV $=$ Yes $\} \rightarrow$ \{Exercise machine $=$ Yes $\}$
(rule 2) $\{H D T V=N o\} \rightarrow$ \{Exercise machine $=$ Yes $\}$ ?
College students:
Confidence of rule $1=1 / 10=10 \%$
Confidence of rule $2=4 / 34=11.8 \%$
Working Adults:
Confidence of rule $1=98 / 170=57.7 \%$
Confidence of rule $2=50 / 86=58.1 \%$



## Correlation is reversed at different levels of generalization

At a more general level of abstraction:
$\{\mathrm{HDTV}=$ Yes $\} \rightarrow$ \{Exercise machine $=$ Yes $\}$

College students:
$\{$ HDTV $=$ No $\} \rightarrow$ \{Exercise machine $=$ Yes $\}$
Working Adults:
$\{$ HDTV $=$ No $\} \rightarrow$ \{Exercise machine $=$ Yes $\}$

This is called Simpson's Paradox

## Importance of Stratification

- The lesson here is that proper stratification is needed to avoid generating spurious patterns resulting from Simpson's paradox.

For example

- Market basket data from a major supermarket chain should be stratified according to store locations, while
- Medical records from various patients should be stratified according to confounding factors such as age and gender.


## Explanation of Simpson's paradox

- Lisa and Bart are programmers, and they fix bugs for two weeks

|  | Week 1 | Week 2 | Both weeks |
| :---: | ---: | ---: | ---: |
| Lisa | $60 / 100$ | $1 / 10$ | $\mathbf{6 1 / 1 1 0}$ |
| Bart | $\mathbf{9 / 1 0}$ | $\mathbf{3 0 / 1 0 0}$ | $39 / 110$ |

Who is more productive: Lisa or Bart?

## Explanation of Simpson's paradox

|  | Week 1 | Week 2 | Both weeks |
| :---: | ---: | ---: | ---: |
| Lisa | $60 / 100$ | $1 / 10$ | $\mathbf{6 1 / 1 1 0}$ |
| Bart | $\mathbf{9 / 1 0}$ | $\mathbf{3 0 / 1 0 0}$ | $39 / 110$ |

If we consider productivity for each week, we notice that the samples are of a very different size

The work should be judged from an equal sample size, which is achieved when the numbers of bugs each fixed are added together

## Explanation of Simpson's paradox

|  | Week 1 | Week 2 | Both weeks |
| :---: | ---: | ---: | ---: |
| Lisa | $60 / 100$ | $1 / 10$ | $\mathbf{6 1 / 1 1 0}$ |
| Bart | $\mathbf{9 / 1 0}$ | $\mathbf{3 0 / 1 0 0}$ | $39 / 110$ |

Simple algebra of fractions shows that even though
$a 1 / A>b 1 / B$
$c 1 / C>d 1 / D$
$(a 1+c 1) /(A+C)$ can be smaller than $(b 1+d 1) /(B+D)!$

This may happen when the sample sizes $A, B, C, D$ are skewed (Note, that we are not adding two inequalities, but adding the absolute numbers)

## Simpson's paradox in real life

- Two examples:
- Gender bias
- Medical treatment


## Example 1: Berkeley gender bias case

Admitted to graduate school at University of California, Berkeley (1973)

|  | Admitted | Not <br> admitted | Total |
| :--- | :--- | :--- | :--- |
| Men | 3,714 | 4,727 | 8,441 |
| Women | 1,512 | 2,808 | 4,320 |

- What's the confidence of the following rules:
(rule 1) $\{$ Man=Yes $\} \rightarrow$ \{Admitted= Yes $\}$
(rule 2) $\{$ Man=No $\rightarrow$ \{Admitted= Yes $\}$ ?
Confidence of rule $1=3714 / 8441=44 \%$
Confidence of rule $2=1512 / 4320=35 \%$
Conclusion: bias against women applicants


## Example 1: Berkeley gender bias case

Stratified by the departments

|  | Men |  | Women |  |
| :--- | :--- | :--- | :--- | :--- |
| Dept. | Total | Admitted | Total | Admitted |
| A | 825 | $62 \%$ | 108 | $82 \%$ |
| B | 560 | $63 \%$ | 25 | $68 \%$ |
| C | 325 | $37 \%$ | 593 | $34 \%$ |
| D | 417 | $33 \%$ | 375 | $35 \%$ |
| E | 191 | $\mathbf{2 8 \%}$ | 393 | $24 \%$ |
| F | 272 | $6 \%$ | 341 | $\mathbf{7 \%}$ |

In most departments, the bias is towards women!

## Example 2: Kidney stone treatment

Success rates of 2 treatments for kidney stones

| Treatments | Success | Not success | Total |
| :---: | ---: | ---: | ---: |
| A* $^{*}$ | 273 | 77 | 350 |
| B** $^{* *}$ | 289 | 61 | 350 |

- What's the confidence of the following rules:
(rule 1) $\{$ treatment $=\mathrm{A}\} \rightarrow$ \{Success= Yes $\}$
(rule 2) $\{$ treatment $=\mathrm{B}\} \rightarrow$ Success $=$ Yes $\}$ ?
(A) Confidence of rule $1=273 / 350=78 \%$
(B) Confidence of rule $2=289 / 350=83 \%$


## Conclusion: treatment B is better

[^0]
## Example 2: Kidney stone treatment

Success rates of 2 treatments for kidney stones

|  | Treatment A | Treatment B |
| :---: | ---: | ---: |
| Small stones | $\mathbf{9 3 \%}(\mathbf{8 1 / 8 7 )}$ | $\mathbf{8 7 \% ( 2 3 4 / 2 7 0 )}$ |
| Large stones | $\mathbf{7 3 \% ( 1 9 2 / 2 6 3 )}$ | $69 \%(55 / 80)$ |
| Both | $\mathbf{7 8 \% ( 2 7 3 / 3 5 0 )}$ | $\mathbf{8 3 \%}(\mathbf{2 8 9 / 3 5 0 )}$ |

Treatment A is better for both small and large stones, But treatment $B$ is more effective if we add both groups together

## Implications in decision making

- Which data should we consult when choosing an action: the aggregated or stratified?
- Kidney stones: if you know the size of the stone, choose treatment $A$, if you don't - treatment $B$ ?


## Implications in decision making

- Which data should we consult when choosing an action: the aggregated or stratified?
- The common sense: the treatment which is preferred under both conditions should be preferred when the condition is unknown


## Implications in decision making

- Which data should we consult when choosing an action: the aggregated or stratified?
- If we always choose to use the stratified data, we can partition strata further, into groups by eye color, age, gender, race ... These arbitrary hierarchies can produce opposite correlations, and lead to wrong choices


## Implications in decision making

- Which data should we consult when choosing an action: the aggregated or stratified?
- Conclusion: data should be consulted with care and the understanding of the underlying story about the data is required for making correct decisions

Negative correlations and flipping patterns

## Negative association rules

- The methods for association mining were based on the assumption that the presence of an item is more important than its absence (asymmetric binary attributes)
- The negative correlations can be useful:
- To identify competing items: absence of Blu ray and DVD player in the same transaction
- To find rare important events: rare occurrence \{Fire=yes, Alarm=On\}


## Mining negative patterns

- Negative itemset: a frequent itemset where at least one item is negated
- Negative association rule: is an association rule between items in a negative itemset with confidence $\geq \operatorname{minConf}$
- If a regular itemset is infrequent due to the low count of some item, it is frequent if we consider the negation (absence) of a corresponding item


## Negative patterns = non-positive



## Challenging task

- Positive associations can be extracted only for highlevels of support. Then the set of all frequent itemsets is manageable
- In this case, the complement to all frequent itemsets is exponentially large, and cannot be efficiently enumerated
- But do we need all negative associations?


## Flipping patterns

- Flipping patterns are extracted from the datasets with concept hierarchies
- The pattern is interesting if it has positive correlation between items which is accompanied by the negative association of their minimal generalizations, and vice versa
- We call such patterns flipping patterns


## Example from Groceries dataset



## Examples from Movie rating dataset



## Examples from US census dataset



## Examples from medical papers dataset




[^0]:    *Open procedures (surgery)
    ** Percutaneous nefrolithotomy (removal through a small opening)

