Cost-based evaluation

Lecture 10

Outline

- Performance measure: error rate
- Generating test set
- Predicting performance interval
- Comparing two classifiers
- Cost-based evaluation

The Inadequacy of Accuracy

- As the class distribution becomes more skewed, evaluation based on accuracy breaks down.
 - Consider a dataset where the classes appear in a 999:1 ratio.
 - A simple rule, which classifies every instance as the majority class, gives a 99.9% accuracy – no further improvement is needed!
- Evaluation by classification accuracy also assumes equal error costs---that a false positive error is equivalent to a false negative error.
 - In the real world this is rarely the case, because classifications lead to actions which have consequences, sometimes grave.

Cost-based evaluation

- In practice, different types of classification errors often incur different costs
- The rare class is often denoted as positive
- The confusion matrix:

		Predict	Predicted class		
		Yes	No		
Actual class	Yes	True positive	False negative		
	No	False positive	True negative		

Terminology

• The *confusion matrix*:

		Predict	Predicted class		
		Yes	No		
Actual class	Yes	True positive	False negative		
	No	False positive	True negative		

True positives (TP) – the number of positive examples correctly predicted as positives False negatives (FN) – the number of positive examples wrongly predicted as negatives False positives (FP) – the number of negative examples wrongly predicted as positives True negatives (TN) – the number of negative examples correctly predicted as negatives

Terminolgy. Fractions

- Suppose you want to know what are all positive instances in your dataset (red dots)
- The classifier outputs as positives the instances inside the oval



Terminology. TPF, sensitivity or recall

- Suppose you want to find all positive instances in your dataset (red dots)
- The classifier outputs as positives the instances inside the oval
- True positive rate (fraction): TPF=TP/all positives
- In the example: 4 red dots out of 10 red dots – TPF=0.4
- Also called: sensitivity or recall
- High sensitivity or high recall mean that classifier found most of the relevant positive instances



Examples:

high-sensitive HIV test- if the person is sick, it will be diagnosed with highprobability

High-recall document query: the query brought most of the relevant documents

Terminology. Precision

- Suppose you want to find all positive instances in your dataset (red dots)
- The classifier outputs as positives the instances inside the oval
- Precision (fraction): precision=TP/(TP+FP)
- In the example: 4 red dots out of 7 total dots which are all identified as positive

Precision=4/7

 High precision means that classifier returned more relevant results than irrelevant



Highly precise HIV test – whoever is classified as HIVpositive is most probably sick

Terminology. False Positive Fraction

- Suppose you want to find all positive instances in your dataset (red dots)
- The classifier outputs as positives the instances inside the oval
- False Positive Rate(fraction): FPF=FP/(all negatives)
- In the example: 3 black dots out of 10 total dots which represent all negative instances

FPF=3/10

 High FPF means that classifier is not very specific – it brings a lot of irrelevant results



Example: mammography

If the person is diagnosed, it is not very likely to be really sick

Terminology. Specificity

- Suppose you want to find all positive instances in your dataset (red dots)
- The classifier outputs as positives the instances inside the oval
- Specificity (fraction): specificity=TN/(all negatives)
- In the example: 7 black dots which are left outside of the positive prediction out of total 10 negative instances

Specificity=7/10

 High specificity means that if classifier identifies something as positive, it is a high probability that it is indeed positive

Specificity + FPF=1.00



Highly-specific test means that it is very low probability to be classified as positive, if the person is indeed negative

Counting the cost. Example

		Predicted class			
		Class + Class -			
Actual	Class +	-1	100		
class	Class -	1	0		

For example, HIV diagnostic test

Cost matrix

 A cost matrix encodes the penalty of classifying records of one class as another. A negative value represents an award for making a correct classification

Counting the cost. Example

		Predicted class			
	Class + Class				
Actual	Class +	-1	100		
class	Class -	1	0		

Cost matrix

		Predicted class				Predicte	d class
		Class +	Class -			Class +	Class -
Actual	Class +	150	40	Actual	Class +	250	45
class	Class -	60	250	class	Class -	5	200

Confusion matrix for Classifier A Confusion matrix for Classifier B

The total cost of model A=150*(-1)+60*1+40*100=3910 The total cost of model B=250*(-1)+5*1+45*100=4255

Counting the cost. Example

		Predicted class			
	Class + Class		Class -		
Actual class	Class +	-1	100		
	Class -	1	0		

Cost matrix

		Predicted class				Predicte	d class
		Class +	Class -			Class +	Class -
Actual	Class +	150	40	Actual	Class +	250	45
class	Class -	60	250	class	Class -	5	200
Classifier A				Class	ifier B		

The total cost of model A=150*(-1)+60*1+40*100=3910 The total cost of model B=250*(-1)+5*1+45*100=4255

• HIV diagnostic test



• Promotional mailing



• Loan decisions



• Fault diagnosis



Cost-based classification

- Let {p,n} be the positive and negative instance classes.
- Let {Y,N} be the classifications produced by a classifier.
- Let c(Y,n) be the cost of a false positive error.
- Let c(N,p) be the cost of a false negative error.
- For an instance *E*,
 - the classifier computes $p(\mathbf{p} | E)$ and $p(\mathbf{n} | E) = 1 p(\mathbf{p} | E)$ and
 - the decision to emit a positive classification is

[1-p(p|E)]*c(Y,n) < p(p|E) * c(N,p)